

# Damage identification of low-density material-filled sandwich panels with truss core based on vibration properties

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## Abstract

A damage-identification method based on flexibility matrix and Teager energy operator is proposed for low-density material-filled sandwich panels with truss core. In the proposed damage index, weight coefficient  $r$  is introduced to consider the effect of damages on both high-order and low-order modes. Numerical simulations and experiments are conducted to assess the performance of the proposed method. Effects of Young's modulus of the filler material on the accuracy of the proposed method are also discussed. Results reveal that the method is reliable and effective for single-damage and multiple-damages identification of filled sandwich panels with truss core, and weight coefficient plays an important role, especially for cases with multiple damages or damages of small extent. Damage identification becomes more difficult as Young's modulus of the filler increases, and there is a critical value, after which the damage could not be identified by the proposed method.

## Keywords

Filled sandwich panels with truss core, damage identification, Teager energy operator, flexibility matrix, filler's influence

## Introduction

As a class of newly developed lightweight multifunctional structure, sandwich panel with truss core (SPTC) is made of two thin face-sheets and one thick lightweight core with various truss configuration, for example, diamond, tetrahedron, kagome, and hourglass.<sup>1–3</sup> This special structural configuration endows the SPTC with many superior properties such as high specific bending stiffness, sound-shock resistance, good thermal insulation, and acoustical isolation.<sup>4–7</sup> For example, it has been considered as one of the most promising candidates to be applied in the thermal protection system (TPS) of high-speed aircrafts. However, various damages or defects may occur in the SPTC during manufacturing process or being in service, including breakage of truss member, burn-through of face-sheets, buckling of the panel, and so on.<sup>8,9</sup> These damages and defects may change the mechanical properties of the SPTC<sup>10</sup> and increase the risk of structure failure. Therefore, damage detection in the early stage is of great importance in avoiding catastrophic events. In practical applications, low-density or porous functional material are often

filled in the void space of the SPTC between the two face-sheets, in order to further enhance the performance in shock resistance,<sup>11,12</sup> thermal insulation, or acoustical isolation.<sup>13,14</sup> The filled material, which may additionally hinder direct visual inspection and significantly alter the dynamic behavior, makes damage identification of the SPTC even difficult.

Recently, non-destructive testing (NDT) methods are developed to detect damages in various sandwich structures, such as acoustic emission (AE),<sup>15,16</sup> electrical impedance,<sup>17</sup> thermography,<sup>18–20</sup> and guided wave.<sup>21–23</sup>

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For sandwich composite structures, Sikdar et al.<sup>16</sup> propose an AE-based real-time health-monitoring framework to identify the probable damage locations. Wong et al.<sup>17</sup> used an electrical impedance resonance shift method to identify the defect accurately in honeycomb core sandwich structures because damages can cause a disrupted change of imaginary part of electrical impedance. Li et al.<sup>21</sup> proposed a novel multi-dimensional signal-processing and mode-tracking approach with a reference-free perspective for the damage identification and localization in the media with large attenuation fact. And the results reflected that the methods offered high accuracy for locating damage positions.

Besides, some vibration-based methods<sup>24,25</sup> are recently introduced to inspect the health status of the sandwich structures. Lestari and Qiao<sup>26</sup> used variation of dynamic responses between healthy and damaged structures to identify damages of fiber-reinforced polymer sandwich composites. Tian et al.<sup>27</sup> utilized uniform load surface (ULS) curvature to detect delamination defects of the lattice sandwich plate. For honeycomb sandwich beams, Zhu et al.<sup>28</sup> propose a vibration-based method by using the frequency response function (FRF) measured at one point. Seguel and Meruane<sup>29</sup> used high-speed three-dimensional (3D) digital image correlation (DIC) system to identify the debonding of the honeycomb sandwich panel. For composite SPTCs, Li et al.<sup>30</sup> propose a ULS-based method, gapped smoothing method (GSM), and Teager energy operator (TEO). Lu et al.<sup>31</sup> propose a baseline-free identification method to identify damages in metallic SPTCs, which utilized the flexibility matrix and GSM. Later on, an improved method was also presented to identify unbound nodes damages.<sup>32</sup>

Recently, low-density thermal insulation material has been filled in the SPTC, and it is found that the filled SPTC has much better performance in thermal insulation, especially in the cases of ultra-high local heat flux, for example, irradiated by high-power laser.<sup>33,34</sup> Compared with plates and pipes, the filled SPTC is more complicated, which consists of two face-sheets, truss core, and filled material. The traditional NDT methods may not work, such as AE and guided wave. Besides, there are many kinds of filled material, such as polymer or metallic foams, porous ceramic, and silicone resin and carbon powder. The material property of the filled material may influence the effectiveness of the damage-identification method. Up to now, there is few, even no, reported work on the damage identification of the low-density material-filled SPTC.

In this article, a vibration-based damage-identification method is proposed for low-density material-filled SPTCs. The damage index  $DIT_r$  is based on the variation of flexibility matrix, and  $r$  is a weight coefficient,

which is to consider effects of damages on both low-order and high-order modes. Numerical simulations and experiments are conducted to investigate effectiveness of the method in identification of single damage and multiple damages with different extents, and the effect of the Young's modulus of the filler is also discussed.

## Damage-identification method

The flexibility matrix  $F$  of a structural system with  $n$  degrees-of-freedom can be expressed as

$$F = \sum_{p=1}^n \frac{\Phi_p \Phi_p^T}{\omega_p^2} \quad (1)$$

where  $\omega_p$  and  $\Phi_p$  are the  $p$ th natural frequency and mode shape, respectively. The contribution of  $p$ th mode on the flexibility matrix  $F_p$  can be written as

$$F_p = \frac{\Phi_p \Phi_p^T}{\omega_p^2} \quad (2)$$

Take  $MD(i)$  as the modal deflection at point  $i$  under uniform unit load all over the structure, for a linear system, it can be approximately deduced as

$$MD(i) = \sum_{p=1}^n \frac{\Phi_p(i) \sum_{j=1}^n \Phi_p(j)}{\omega_p^2} \quad (3)$$

For a linear system, the definition of ULS is expressed as the deflection vector of the structure under uniform load

$$MD = \{MD(i)\} = \sum_{p=1}^n F_p I = \sum_{p=1}^n MD_p \quad (4)$$

where  $I$  is  $\{1, \dots, 1\}^T$   $1 \times n$ .  $MD_p$  is the  $p$ th-order mode contribution to  $MD$ .

When a specimen is damaged, the vibration characteristics would change. In the work, variation of  $MD_p$  is defined as

$$\begin{aligned} DI &= \sqrt{\sum_{p=P_1}^{P_2} (MD_{pD} - MD_{pU})^2} \\ &= \sqrt{\sum_{p=P_1}^{P_2} ([F_p \cdot I]_D - [F_p \cdot I]_U)^2} \end{aligned} \quad (5)$$

where  $P_1$  and  $P_2$  are the beginning- and the ending-order modes in the practical case.  $MD_{pD}$  and  $MD_{pU}$

denote the  $p$ th component of modal deflection of the damaged and undamaged models, respectively.

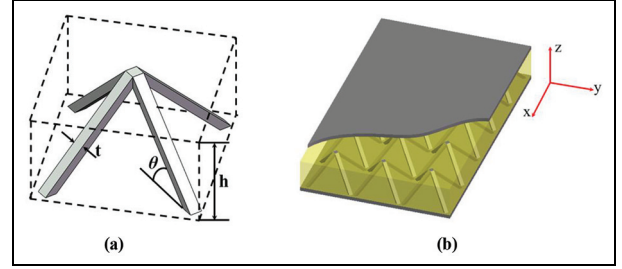
According to the definition of  $MD_p$ , weight of low-order modes is larger than that of high-order modes. However, higher-order modes are more sensitive to local damages.<sup>35</sup> To identify various damages, the damage index  $DI_r$  is defined

$$DI_r = \sqrt{\sum_{p=P_1}^{P_2} \alpha_p^r (MD_{pD} - MD_{pU})^2} \quad (6)$$

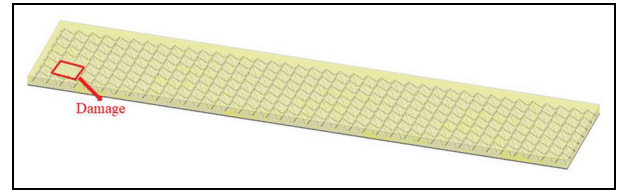
where  $\alpha_p^r$  is expressed as the weight coefficient of the  $p$ th component

$$\alpha_p^r = \frac{\omega_p^r}{\sum_{p=P_1}^{P_2} \omega_p^r} \quad (7)$$

$\alpha_p^r$  could determine the weights of low-order and high-order modes in  $DI_r$ , and  $r$  is an integer. When  $r$  is less than 2, the weight of low-order modes in  $DI_r$  is larger than that of high-order modes. When  $r$  is equal to 2, the weight of low-order modes in  $DI_r$  is equal to the weight of high-order modes. When  $r$  is larger than

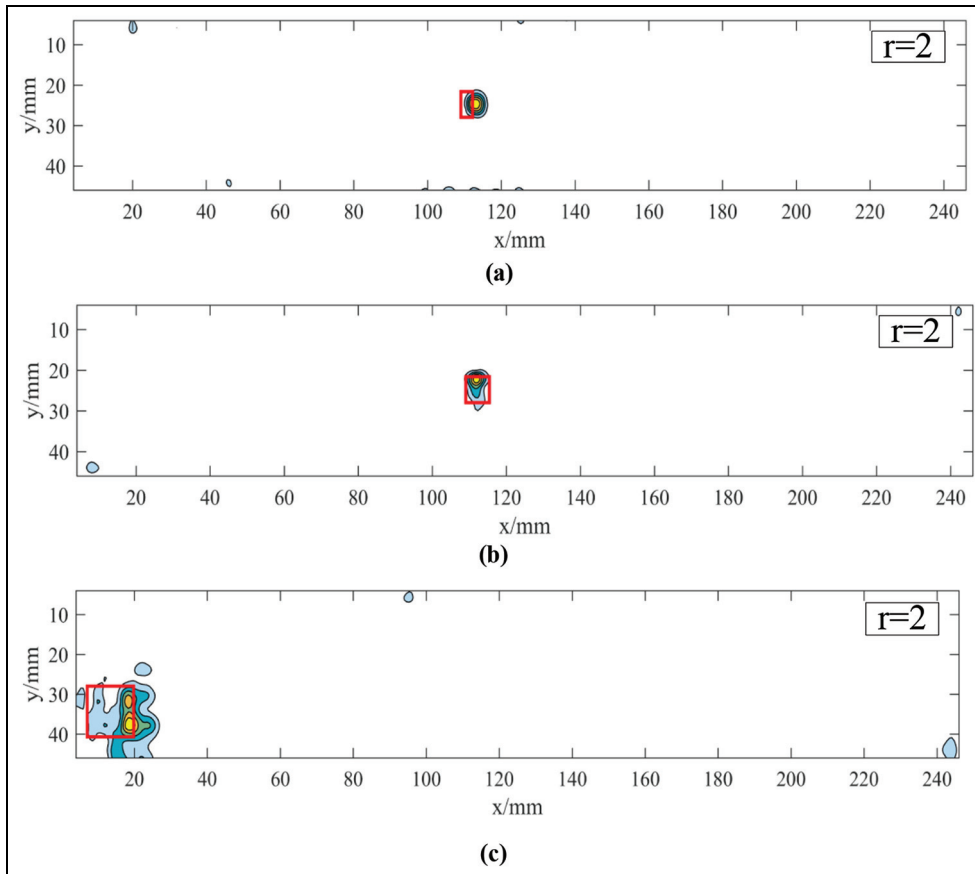


**Figure 1.** Model information: (a) unit cell of pyramidal truss and (b) the filled sandwich panel.

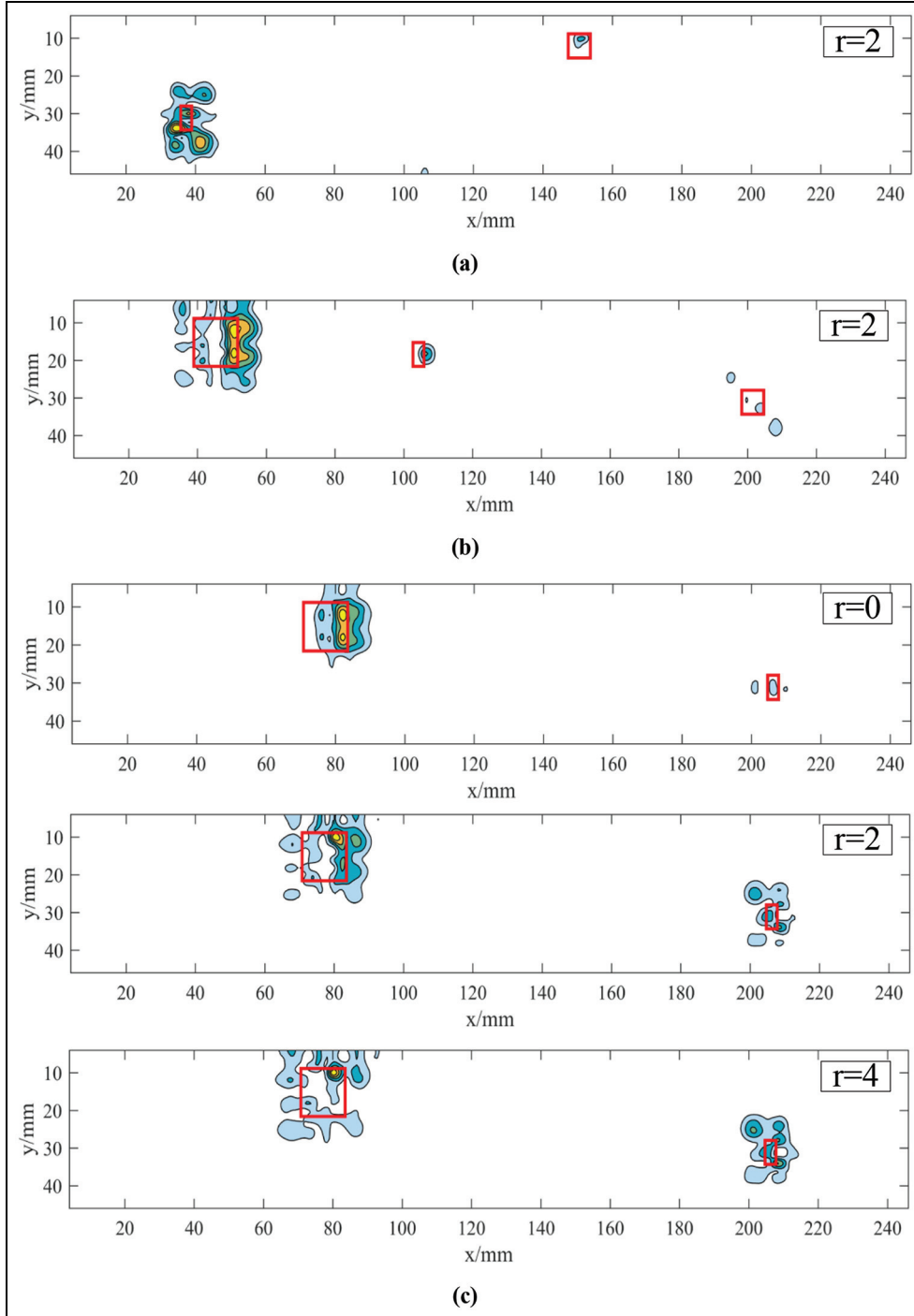


**Figure 2.** Example of damaged specimen.

2, the weight of low-order modes in  $DI_r$  is smaller than that of high-order modes.



**Figure 3.** Results of  $DIT_2$ : (a) S1, (b) S2, and (c) S3.



**Figure 4.** Results of  $DIT_r$ : (a) M1, (b) M3, and (c) M2.

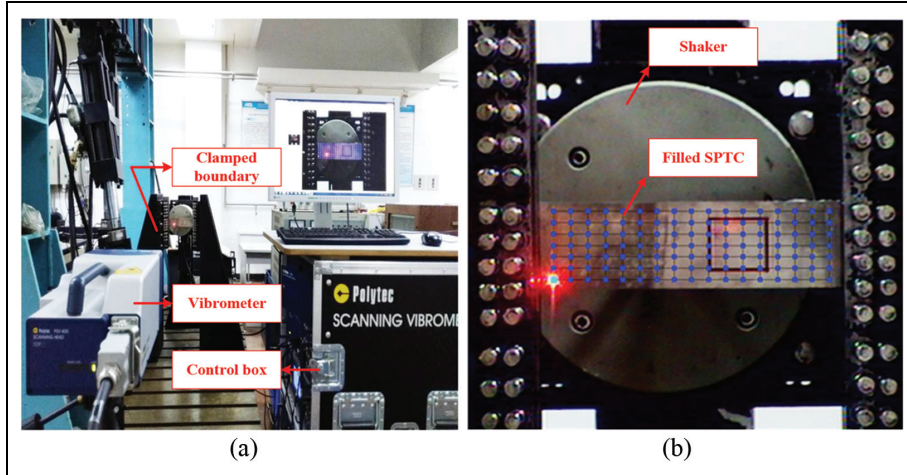
In order to suppress the global fluctuation and singularities caused by non-damage factors (boundary conditions, contact nodes, etc.), TEO is used to process damage index  $DI_r$ , and then the index  $DIT_r$  can be obtained. The damage index  $DIT_r$  for spatial sampling points can be defined as equation (8). In the work, damage index  $DIT_0$ ,  $DIT_2$  and  $DIT_4$  are selected to identify damages of SPTCs

$$DIT_r(k) = |DI_r^2(k) - DI_r(k-1)DI_r(k+1)| \quad (8)$$

## Numerical simulation

### Numerical model

The sketch of the filled pyramid SPTC model being simulated is shown in Figure 1. Figure 1(a) gives the



**Figure 5.** Experiment information: (a) experimental setup and (b) scanning points.

unit cell of pyramidal truss, where  $h = 4$  mm,  $\theta = 45^\circ$ ,  $t = 0.5$  mm. Figure 1(b) gives the illustration of low-density material filled SPTC. The filled material is silicone resin mixed with carbon powder, which is a typical lightweight ablation resistance material. Young's modulus and density of silicone resin mixed with carbon powder could be changed according to the proportion of carbon powder.

A typical damaged specimen is shown in Figure 2, and there are 7 units and 39 units along the  $x$  and  $y$  directions, respectively. The thickness of the face-sheet is 0.5 mm. The SPTC is made of stainless steel with Young's modulus of 200 GPa, Poisson ratio of 0.3, and mass density of  $7800 \text{ kg/m}^3$ . Young's modulus of the filled material is 100 MPa, Poisson ratio is 0.3, and mass density is  $1100 \text{ kg/m}^3$ . The boundary condition is two sides clamped and two sides free (CCFF).

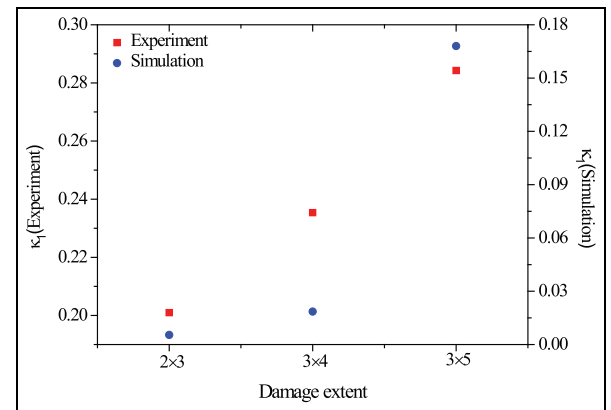
In the article, cell missing damages are considered and cases of single damage and multiple damages of different extents are simulated. The example of damaged model is given in Figure 2. Cases of single damage include half-cell missing (S1), one-cell missing (S2), and  $2 \times 2$  cells missing (S3). And cases of multiple damages include one and half cells (M1); half-cell and  $2 \times 2$  cells missing (M2); half-cell, one-cell, and  $2 \times 2$  cells missing (M3). Damage locations in single-damage and multiple-damages cases are selected randomly. The first 10 order modes are used to calculate damage index  $DIT_r$ .

### Single-damage identification

Identification of single damage with different extents is conducted.  $DIT_2$  results are provided in Figure 3, and the red rectangle is the actual damage region. From Figure 3, it is understood that the proposed method could identify the single damage with different extents



**Figure 6.** The damaged specimen: DS  $2 \times 3$ .

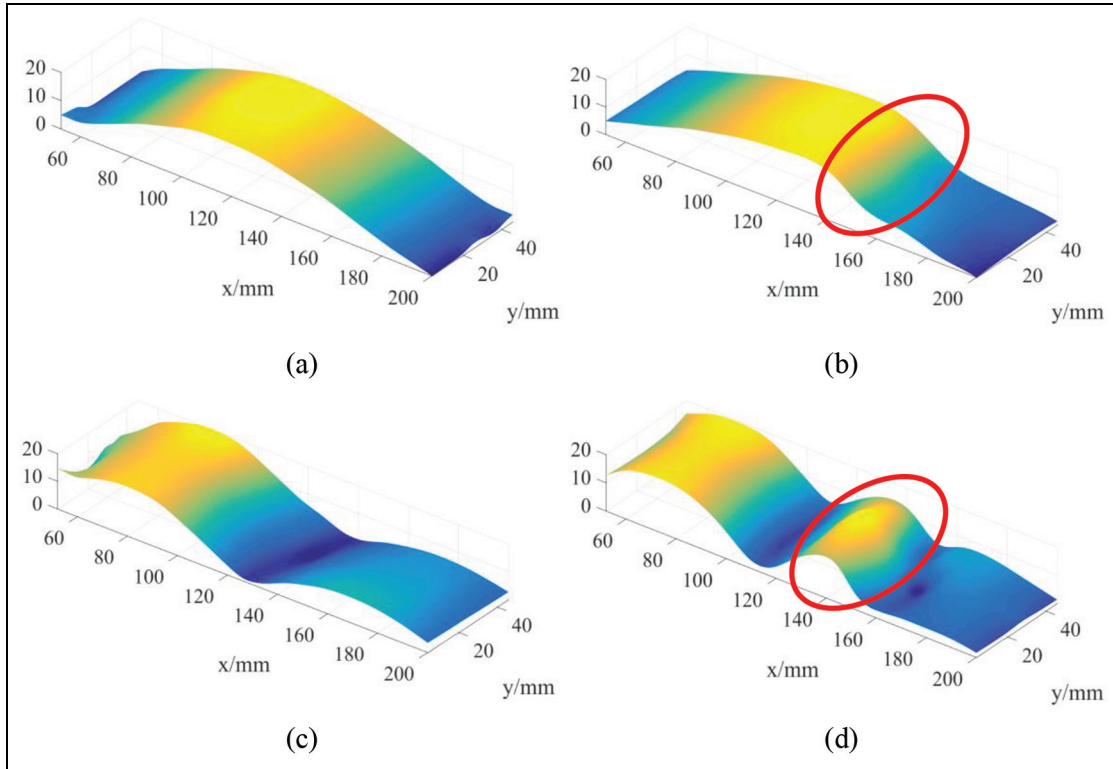


**Figure 7.**  $\kappa_1$  results of simulations and experiments.

effectively, no matter where the damage is. Besides, as the extent of damages increases from S1 to S3, influences of damages on their surroundings also increases, demonstrating that the proposed damage index is sensitive to damage extent.

### Multiple-damages identification

In order to verify the effectiveness of the method in multiple-damages identification, three damaged models



**Figure 8.** Tested mode shapes. (a) and (b): first mode shape of US and DS  $2 \times 3$ . (c) and (d): second mode shape of US and DS  $2 \times 3$ .

of filled pyramid SPTCs (named M1, M2, and M3) are used, and results are shown in Figure 4. The red rectangles represent the actual damage regions.

From Figure 4(a)–(c), all damages could be identified accurately, no matter whether there are two or three damages. To investigate the effect of weight coefficient on damage identification, results of M2 in the case of different  $r$  are provided in Figure 4(c). From Figure 4(c), it is found that with the increasing of the weight coefficient, half-cell missing becomes more obvious. As small-extent damages normally have greater influences on higher-order modes than the lower-order modes. It reveals that high-order modes should be considered to locate damages of small extent. Besides, comparing results in the case of  $r = 0$  and  $r = 4$ , it is also found that the extent identification is more accurate when  $r = 0$ , whereas it is easier to locate the damage of small extent when  $r = 4$ . Therefore, results in the case of different weight coefficient should be combined together to improve the accuracy of both damage location and damage extent identification.

Moreover, from Figure 4(a), although the damage extent of half-cell missing is smaller than that of one-cell missing, the affected area of half-cell missing is much larger than that of one-cell missing. According to half-cell missing results in Figure 4(a)–(c), it is seen that

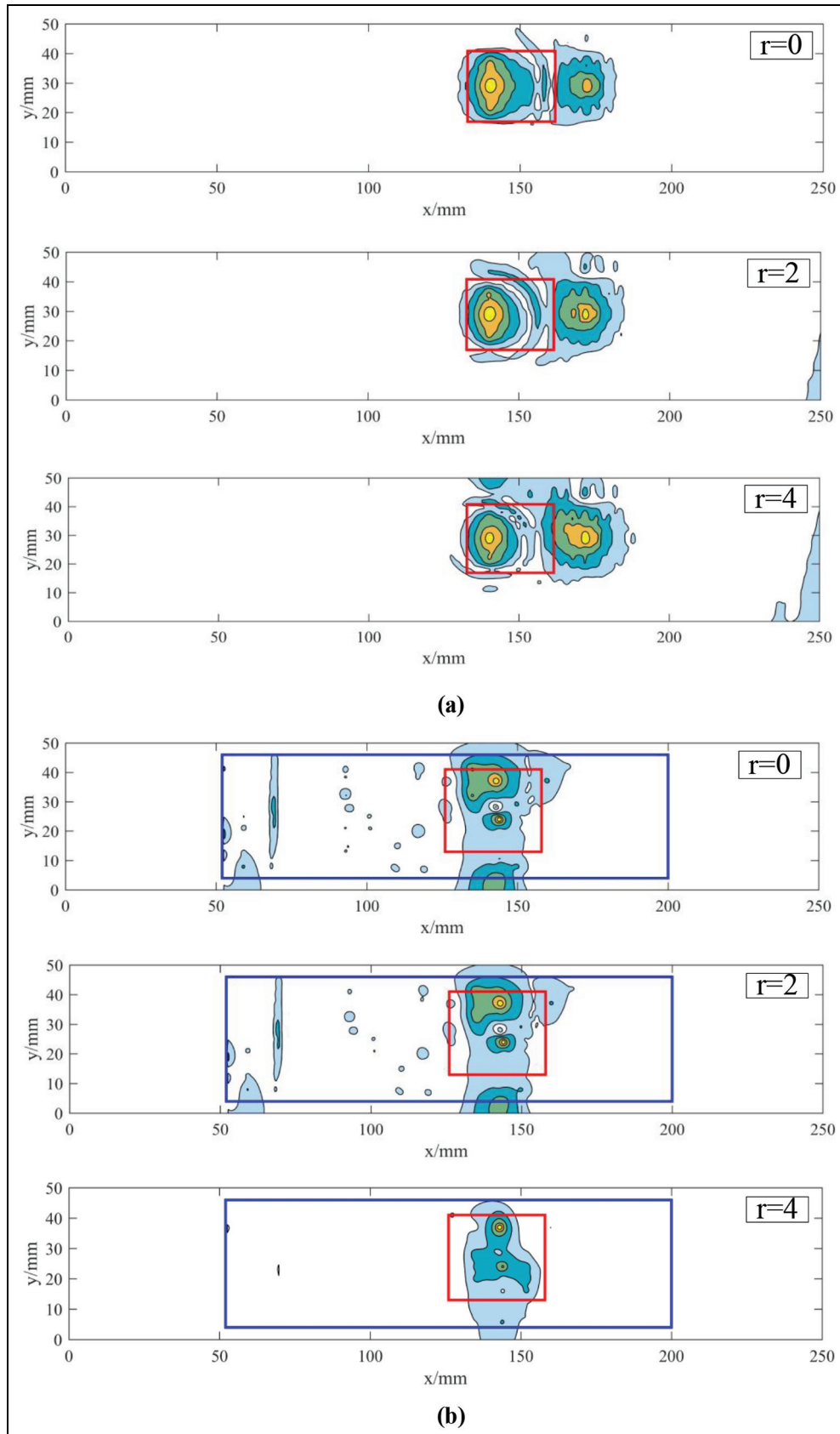
the same extent damages at different locations would have different influences on structural modes or damage indexes. Besides, when the damage extent is the same, variations of modal information caused by damages at the boundary are normally larger than that caused by damages away from boundary. The result is in accordance with Lu et al.,<sup>10</sup> and Lou et al.<sup>35</sup>

## Experimental study

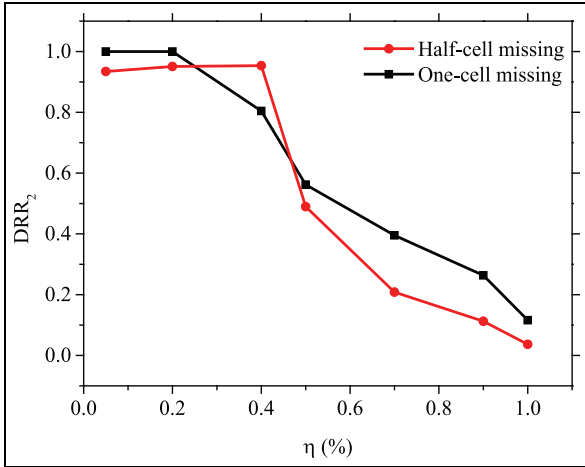
### Experimental setup

To verify the effectiveness of the proposed method and numerical model, experiments are also conducted. The experimental setup is shown in Figure 5(a). The specimens of metallic SPTCs with the filler are excited by a shaker (JZK-50). Two edges of the specimens are clamped. The excitation signal is generated by the control system of the laser Doppler vibrometer (Polytec, PSV-400) and amplified by a power amplifier (YE5872A) before input to the shaker. The frequency bandwidth of the excitation signal is set in the range of 1–4 kHz with the resolution of 625 mHz.

The laser Doppler vibrometer is applied to measure the structural vibration response, and the scanning points are focused on the front face-sheet, as shown in



**Figure 9.** Identification results of  $DS\ 2 \times 3$ : (a) simulation and (b) experiment.



**Figure 10.**  $DRR_2$  results.

Figure 5(b). The other side of the face-sheet is connected to the shaker by metallic bar. The obtained excitation and structural response signal are used to calculate the FRF to get structural modal information.

### The preparation of specimens

In this work, the metallic pyramid truss cores with a relative density  $\rho$  of about 3% are fabricated from 0.7-mm thick perforated stainless steel sheet by folding technique. The brazing technique is utilized to join the truss core with face-sheets. The dimension of the filled specimen is 50 mm  $\times$  250 mm. The thickness of the face-sheet is 0.9 mm and the truss core is 7 mm. The lightweight ablation-resistant material, that is, silicone resin mixed with carbon powder, is filled into the pre-fabricated healthy and damaged pyramidal SPTCs, and the filler's density is 0.2 kg/m<sup>3</sup>.

In the tests, cell missing damages are considered and truss core cells of the damaged location are cut out before brazing. Damages with different sizes and locations are considered. Undamaged specimen is named US, and the specimens with cells missing are named DS. The damage sizes include 2  $\times$  3 cells missing, 3  $\times$  4 cells missing, and 3  $\times$  5 cells missing, named DS 2  $\times$  3, DS 3  $\times$  4, and DS 3  $\times$  5, respectively. The specimen DS 2  $\times$  3 is shown in Figure 6, and the red rectangle represents the damaged region.

### Experimental results

The differential ratio of natural frequency  $\kappa_i$  is defined to validate the numerical model

$$\kappa_i = \frac{|f_i^U - f_i^D|}{f_i^U} \quad (9)$$

where  $f_i^U$  is the  $i$ th natural frequency of the undamaged model,  $f_i^D$  is the  $i$ th natural frequency of the damage model.

The numerical models, having the same damage extents with the experimental models, are built, and the  $\kappa_1$  results of both numerical simulations and experiments are presented in Figure 7. From Figure 7, although the values of  $\kappa_1$  of experiments are different from those of simulations, the tendency of parameter  $\kappa_1$  of numerical model is in accordance with that of experiment as the damage extent increases. Many factors contribute to the difference between simulation and experiment. For example, the boundary condition of numerical model is ideal and strict. However, the boundary condition of experimental model is not ideal, and it may loosen a little as the structure vibrates. The manufacturing process of the specimens may also induce errors.

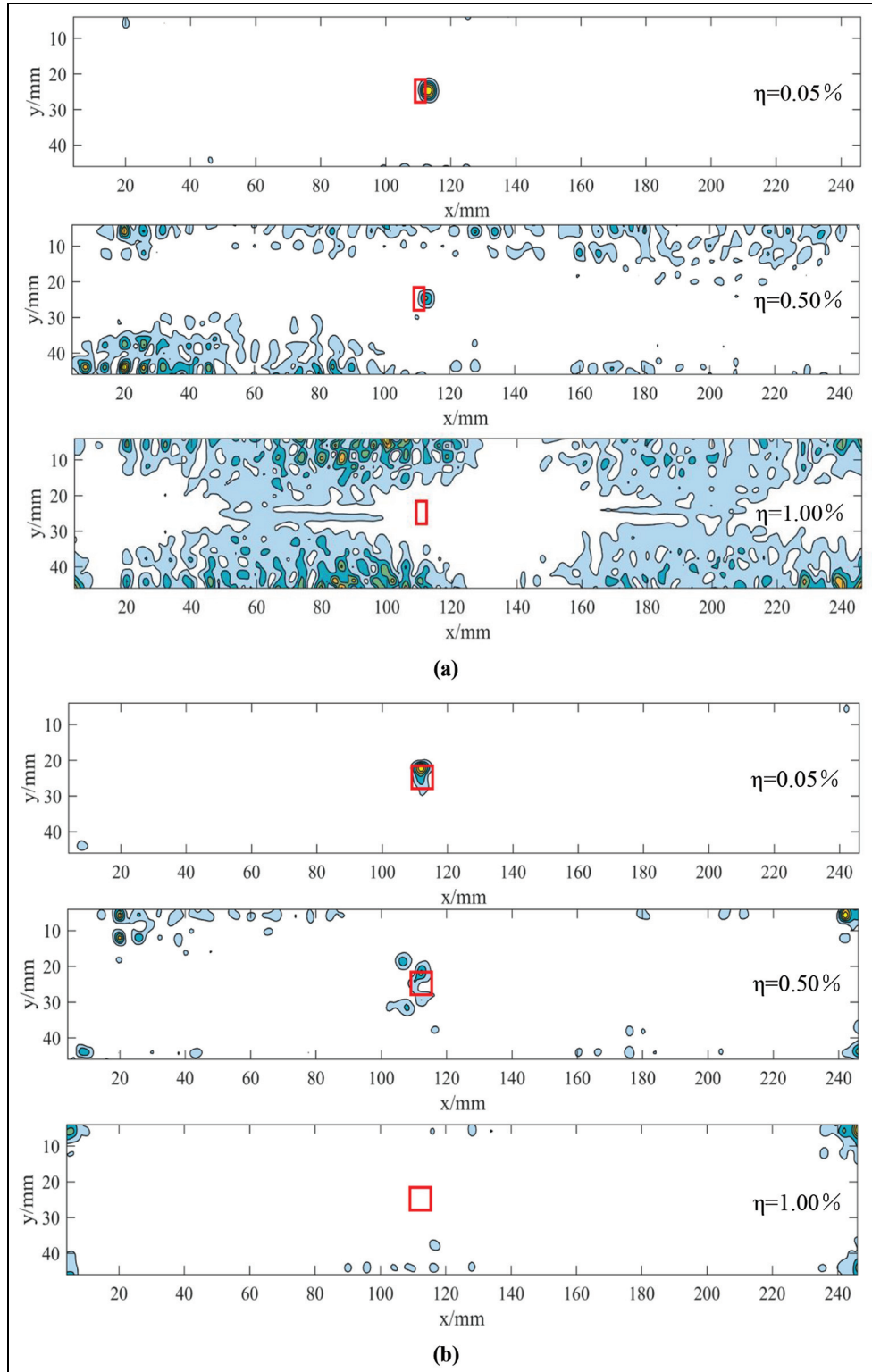
The first two tested modes of US and DS 2  $\times$  3 are provided in Figure 8. After the specimen is damaged, the vibration property of the local damaged zone is different from that of a US, as the red circles shown in Figure 8. After the mode shapes are obtained, the damage index is calculated based on the first 2 mode shapes, and results are shown in Figure 9.

The identification results of the most representative specimen, DS 2  $\times$  3, are shown in Figure 9. The length of the restrict edge is 40 mm; therefore, the real measured region is small and as the blue rectangle shown in Figure 9(b). To compare with numerical results, the x and y coordinate of the experimental results are extended. It is observed from Figure 9 that the damage could be identified effectively according to the numerical and experimental results. The difference between the simulations and experiments are induced by the boundary condition and the manufacturing process of the specimens.

### Discussion

According to the dynamic theory, Young's modulus and density of the filler would affect dynamic property of the whole SPTC and then affect the damage identification. In the article, the influence of Young's modulus of the filler on damage identification is discussed. Filled SPTCs with half-cell missing and one-cell missing are employed to investigate the effect of the filler. In the work, when Young's modulus of the filler is 100, 400, 700, 1000, 1400, 1700, and 2000 MPa, the corresponding numerical model is analyzed, and the results are shown in Figures 10 and 11. In order to investigate the effect of Young's modulus of the filler quantitatively, the damage-recognition rate  $DRR_r$  is defined as





**Figure 11.**  $DIT_2$  results of damaged specimens with different Young's modulus of the filler: (a) half-cell missing and (b) one-cell missing.

$$DRR_r = \frac{DIT_{\max,r}^D}{DIT_{\max,r}^W} \quad (10)$$

where  $DIT_{\max,r}$  is the maximum  $DIT_r$  value in the whole face-sheet.  $DIT_{\max,r}^D$  is the maximum  $DIT_r$  value in the damaged region.

Parameter  $\eta$  is defined as

$$\eta = \frac{E_f}{E_{BM}} \quad (11)$$

where  $E_f$  and  $E_{BM}$  are Young's modulus of filler and base material of SPTC, respectively.

$DRR_2$  results of the two damaged models, specimens with half-cell missing and one-cell missing are provided in Figure 10. It is clearly noted that  $DRR_2$  decreases as Young's modulus of the filler increases. When the  $DRR_2$  is around 1, it demonstrates that the damage can be identified completely, as shown in the first line figures of Figure 11(a) and (b). When the  $DRR_2$  is around 0.5, the damage becomes invisible, as the figures in the case of  $\eta = 0.5\%$  shown. When the  $DRR_2$  is less than 0.5, the real damage is completely unidentified. For the cases with half-cell and one-cell missing, when  $\eta$  is larger than 0.5%, the real damage could not be identified according to the proposed method.

When damage extent increases or the damage location changes, the critical  $\eta$  may change. And more work will be done to investigate effect of material property of the filler on the damage identification of filled SPTC.

## Conclusion

Low-density material-filled SPTC is the primary form of this type of sandwich panel during engineering practice. The filled functional material further enhances the performance of SPTC. However, it also presents new challenges in damage identification of filled SPTC. In this article, a vibration-based method is presented to detect damages in the filled SPTC. Weight coefficient  $r$  is used to consider effects of damages on both high-order modes and low-order modes. Numerical simulations and experimental validations are conducted to assess effectiveness of the proposed method. Moreover, the effect of material property of the filler on the method is also discussed. Some conclusions can be drawn as follows:

1. The proposed method can identify both single damage and multiple damages with different extents effectively. The proposed weight coefficient  $r$  can improve the effectiveness of the method, especially for identification of multiple damages or damages with small extent. For small-extent damages, results in the case of different weight coefficients must be combined together to improve the accuracies of both damage location and extent identification.
2. Local damage identification becomes more difficult as Young's modulus of the filler increases. For half-cell and one-cell damage, the critical  $\eta$  is

around 0.5%. When the damage extent or damage location changes, the critical  $\eta$  may also change. More works must be done to study the effect of Young's modulus of the filler.

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